

*First Postulate:* At a fixed time  $t_0$ , the state of a physical system is defined by specifying a ket  $|\psi(t_0)\rangle$  belonging to the state space  $\mathcal{E}$ .

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*Second Postulate:* Every measurable physical quantity  $\mathcal{A}$  is described by an operator  $A$  acting in  $\mathcal{E}$ ; this operator is an observable.

*Third Postulate:* The only possible result of the measurement of a physical quantity  $\mathcal{A}$  is one of the eigenvalues of the corresponding observable  $A$ .

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*Fourth Postulate (case of a discrete spectrum):* When the physical quantity  $\mathcal{A}$  is measured on a system in the normalized state  $|\psi\rangle$ , the probability  $\mathcal{P}(a_n)$  of obtaining the eigenvalue  $a_n$  of the corresponding observable  $A$  is:

$$\mathcal{P}(a_n) = \sum_{i=1}^{g_n} |\langle u_n^i | \psi \rangle|^2$$

where  $g_n$  is the degree of degeneracy of  $a_n$  and  $\{ |u_n^i\rangle \} (i = 1, 2, \dots, g_n)$  is an orthonormal set of vectors which forms a basis in the eigensubspace  $\mathcal{E}_n$  associated with the eigenvalue  $a_n$  of  $A$ .

*Fifth Postulate:* If the measurement of the physical quantity  $\mathcal{A}$  on the system in the state  $|\psi\rangle$  gives the result  $a_n$ , the state of the system immediately after the measurement is the normalized projection,  $\frac{P_n |\psi\rangle}{\sqrt{\langle \psi | P_n | \psi \rangle}}$ , of  $|\psi\rangle$  onto the eigensubspace associated with  $a_n$ .

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*Sixth Postulate:* The time evolution of the state vector  $|\psi(t)\rangle$  is governed by the Schrödinger equation:

$$i\hbar \frac{d}{dt} |\psi(t)\rangle = H(t) |\psi(t)\rangle$$

where  $H(t)$  is the observable associated with the total energy of the system.