

Chem M3LC. R. Corn

Diprotic Weak Acid

Constants: K_1 , K_2 , K_w , C_{tot}

Five species: $[H_2A]$, $[HA^-]$, $[A^{2-}]$, $[H^+]$, $[OH^-]$

$$K_1 = [H^+][HA^-]/[H_2A] \quad \text{acid dissociation 1}$$

$$K_2 = [H^+][A^{2-}]/[HA^-] \quad \text{acid dissociation 2}$$

$$K_w = [H^+][OH^-] \quad \text{water dissociation}$$

$$[H^+] = [HA^-] + 2[A^{2-}] + [OH^-] \quad \text{charge balance}$$

$$C_{tot} = [H_2A] + [HA^-] + [A^{2-}] \quad \text{mass balance}$$

Alpha Fractions

$$[H_2A]/C_{tot} = (1 + K_1/[H^+] + K_1K_2/[H^+]^2)^{-1}$$

$$[HA^-]/C_{tot} = ([H^+]/K_1 + 1 + K_2/[H^+])^{-1}$$

$$[A^{2-}]/C_{tot} = ([H^+]/K_2 + [H^+]^2/K_1K_2 + 1)^{-1}$$

Iterative eqns for $[H^+]$

$$[H^+][HA^-] = K_1[H_2A]$$

$$[H^+]([H^+] - [OH^-] - 2[A^{2-}]) = K_1[H_2A]$$

$$[H^+]^2 - 2[H^+][A^{2-}] - K_w = K_1[H_2A]$$

$$[H^+]^2 = K_1[H_2A] + 2K_2[HA^-] + K_w$$

$$\text{Initial Guess: } [H^+] = \sqrt{K_1 * C_{tot} + K_w}$$

Calculate $[H_2A]$, $[HA^-]$, $[A^{2-}]$

$$[H^+] = \sqrt{K_1[H_2A] + 2K_2[HA^-] + K_w}$$