Concentrations

Major ionic species in seawater

Pacific Ocean Water Concentrations / mg L ⁻¹		Cl 536 mM
mg L		
lon	CRC values ^a	Na+ - 457 mM
Na⁺	1.05×10^4	
K⁺	3.80×10^2	Mg ²⁺ - 56.3 mN
Mg ²⁺	1.35 × 10 ³	SO ₄ ²⁻ - 27.6 mN
Ca ²⁺	4.00 × 10 ²	Ca ²⁺ - 10.0 mM
Cl⁻	1.90 × 10 ⁴	Ca2+ - 10.0 m/vi
SO ₄ ²⁻	2.65 × 10 ³	K+ - 9.74 mM
Br ⁻	6.5 × 10 ¹	Br 0.823 mM

^aCRC Handbook of Chemistry and Physics, 61st ed.

Chem M3LC R. Corn

Concentrations	Relative molar amounts	
Cl 536 mM	1000	
Na+ - 457 mM	853	
Mg ²⁺ - 56.3 mM	105	
SO ₄ ²⁻ - 27.6 mM	51.5	Chemists use molarity!
Ca ²⁺ - 10.0 mM	18.7	
K+ - 9.74 mM	18.2	
Br 0.823 mM	1.54	

Chem M3LC R. Corn

$$SO_4^{2-}$$
 I. Turbidity Measurements for Sulfate

$$Mg^{2+}$$
 3. Magnesium Complexometric Fluorometry

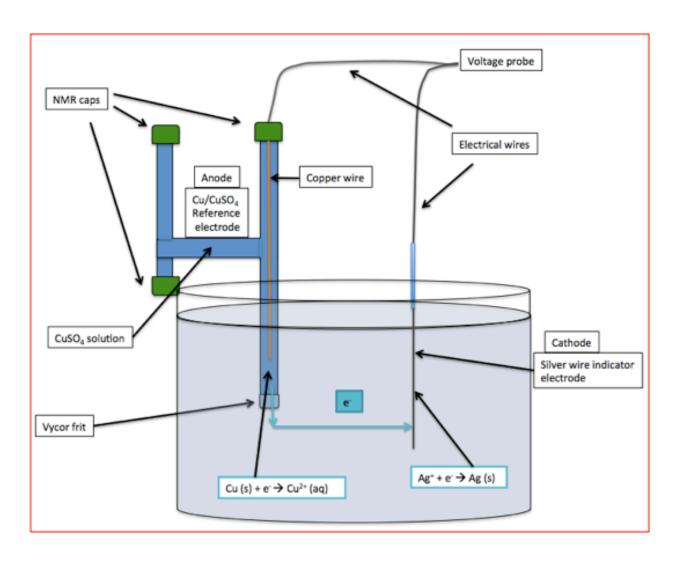
$$Mg^{2+}$$
 Ca^{2+} 4. EDTA titrations for Magnesium and Calcium

Precipitation Reactions: Detection Methods

AgCl(s) Precipitation Titration

BaSO₄(s) Turbidity

 $(C_6H_5)4BK$ Turbidity



$$Ag^{+}(aq) + Cl^{-}(aq) \leftrightharpoons AgCl(s)$$

R. Corn Chem M3LC Fall 2013

In this experiment, silver ions will be added to a chloride solution. As Ag⁺ is added to the Cl⁻, AgCl will form as follows:

$$Ag^{+}(aq) + Cl^{-}(aq) \rightleftharpoons AgCl(s)$$

This equation illustrates the solubility equilibrium of silver chloride. Solubility equilibrium exists when a solid compound is in equilibrium with the dissolved ions of that compound. The corresponding solubility constant of AgCl is:

$$K_{sp} = [Ag^+][Cl^-] = 1.8 \times 10^{-10}$$

The equilibrium constant, K_{T_i} of the titration is:

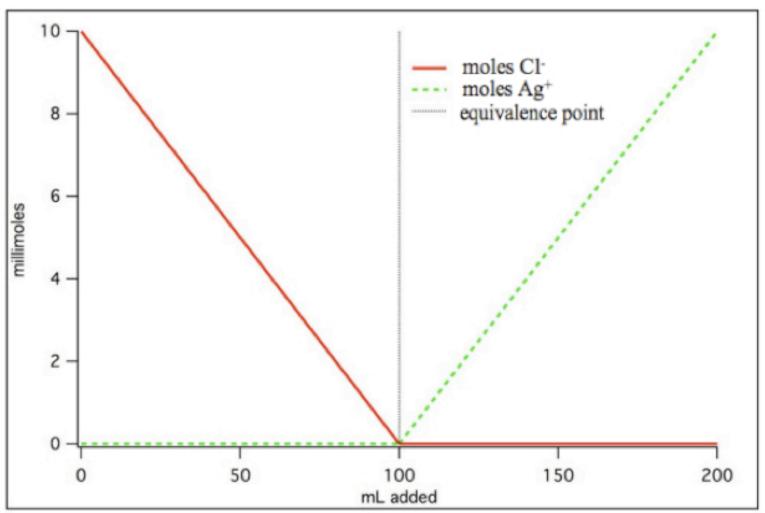
$$K_{\rm T} = \frac{1}{[Ag^+][Cl^-]} = \frac{1}{K_{\rm sp}} = \frac{1}{1.8 \times 10^{-10}} \gg 1$$

As the titration proceeds, the number of moles of chloride decreases.

At the equivalence point, the number of moles of Ag⁺ added is equal to the number of moles of Cl⁻ present *initially*.

We will use Electrochemistry to determine the equivalence point.

$$Ag^{+}(aq) + Cl^{-}(aq) \leftrightharpoons AgCl(s)$$



Ag⁺ solution is added to react with Cl⁻

We will use Electrochemistry to determine the equivalence point.

Electrochemical cell

In this experiment, a Cu/CuSO₄ reference electrode will be used in conjunction with a silver wire **indicator electrode**. The oxidation of copper takes place at the anode while the reduction of silver takes place at the cathode. See the Figure for an illustration of the electrochemical cell.

The balanced electrochemical reaction is as follows:

$$Cu^{o}(s) + 2Ag^{+}(aq) \rightarrow 2Ag^{o}(s) + Cu^{2+}(aq)$$

The line notation for the cell is:

$$Cu(s) | Cu^{2+}(0.100 M) | |Ag^{+}(x M) | Ag(s)$$

The overall standard electrochemical potential, E^{o}_{cell} is:

$$E_{cell}^{0} = E_{Ag}^{0} - E_{Cu}^{0}$$

We use the Nernst Equation to calculate the standard cell potential.

$$Cu(s) | Cu^{2+}(0.100 M) | |Ag^{+}(x M) | Ag(s)$$

Silver is being reduced:

$$Ag^{+} + e^{-} \rightarrow Ag(s)$$

$$E_{Ag} = E_{Ag}^{0} - \frac{.0592}{1} \log \left(\frac{1}{[Ag^{+}]}\right)$$

Copper is being oxidized:

$$Cu^{2+} + 2e^{-} \to Cu(s)$$

$$E_{Cu} = E_{Cu}^{0} - \frac{.0592}{2} \log\left(\frac{1}{[Cu^{2}+1]}\right)$$

*Note: we still use reduction reaction to calculate E_{Cu}

$$E_{cell} = E_{Red} - E_{Ox} = E_{Ag} - E_{Cu}$$
 Ecu is constant during the titration

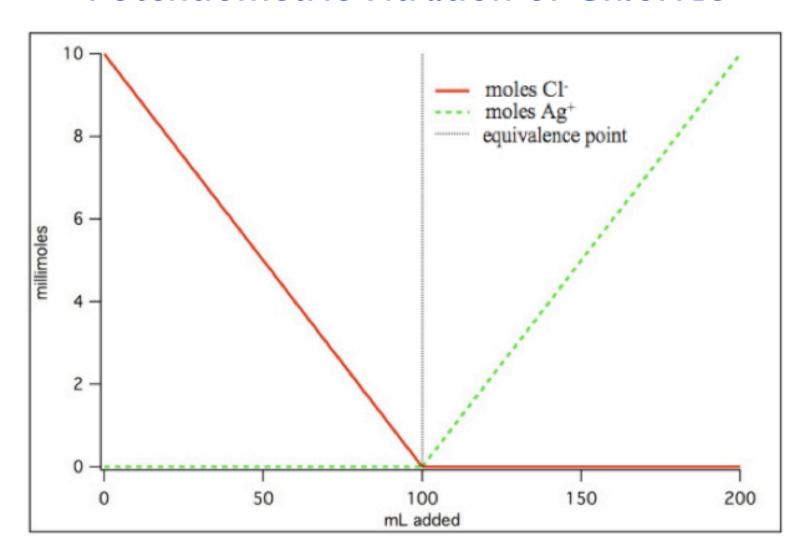
We measure pAg during the titration with potentiometry:

$$pAg = - log [Ag^+]$$

$$E_{cell} = E_{Ag} - E_{Cu}$$

$$E_{cell} = A + B \times pAg$$

A and B are constants



Ag⁺ solution is added to react with Cl⁻

At the equivalence point, [Ag+] and [Cl-] are almost zero, but not quite!

At the eq. pt:
$$K_{sp} = [Ag^{+}][C][C][Ag^{+}] = [C][Ag^{+}] = [C][Ag^{+}][C][Ag^{+}] = [K_{sp}]^{1/2}$$

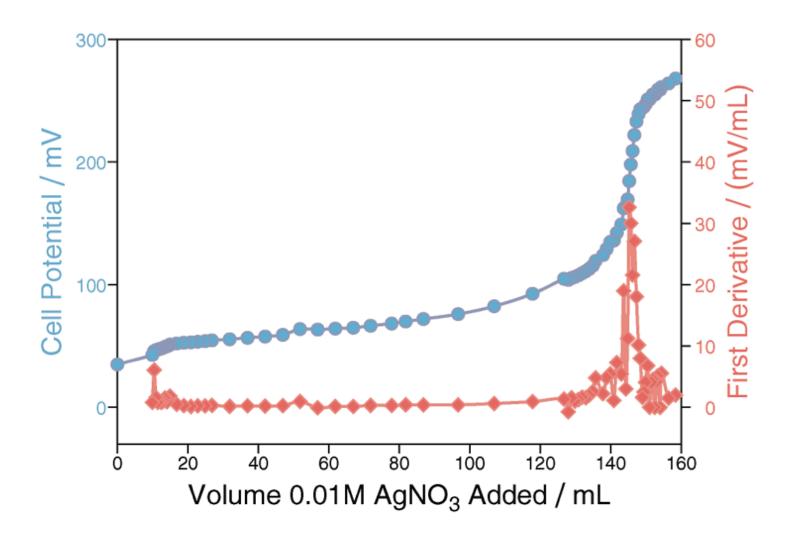
$$pAg = ??$$

At the equivalence point, [Ag+] and [Cl-] are almost zero, but not quite!

At the eq. pt:
$$K_{sp} = [Ag^{+}][C][C][Ag^{+}] = [C][Ag^{+}] = [C][Ag^{+}][C][Ag^{+}] = [K_{sp}]^{1/2}$$

$$K_{sp} = 1.8 \times 10^{-10}$$

pAg = 4.87



Example of Potentiometric Titration Data

$$Zn(OH)_{2(s)} \rightleftharpoons Zn^{2+} + 2OH^{-}$$
 $K_{sp1} = 3 \times 10^{-16}$
 $Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+} + 2OH^{-}$ $K_{sp2} = 7.1 \times 10^{-12}$

Initial Solution has 1.00 mM Zn²⁺ and 1.00 mM Mg²⁺.

I) At what pH does Zinc Hydroxide begin to precipitate?

$$Zn(OH)_{2(s)} \rightleftharpoons Zn^{2+} + 2OH^{-}$$
 $K_{sp1} = 3 \times 10^{-16}$
 $Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+} + 2OH^{-}$ $K_{sp2} = 7.1 \times 10^{-12}$

Initial Solution has 1.00 mM Zn²⁺ and 1.00 mM Mg²⁺.

I) At what pH does Zinc Hydroxide begin to precipitate?

$$[Zn^{2+}] = 1.00 \times 10^{-3}M$$
 $K_{sp1} = [Zn^{2+}][OH^{-}]^{2}$

$$Zn(OH)_{2(s)} \rightleftharpoons Zn^{2+} + 2OH^{-}$$
 $K_{sp1} = 3 \times 10^{-16}$
 $Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+} + 2OH^{-}$ $K_{sp2} = 7.1 \times 10^{-12}$

Initial Solution has 1.00 mM Zn²⁺ and 1.00 mM Mg²⁺.

I) At what pH does Zinc Hydroxide begin to precipitate?

$$[Zn^{2+}] = 1.00 \times 10^{-3}M$$
 $K_{sp1} = [Zn^{2+}][OH^{-}]^{2}$

$$[OH^{-}] = \sqrt{\frac{K_{sp1}}{[Zn^{2+}]}} = \sqrt{\frac{3 \times 10^{-16}}{10^{-3}}} = 5.48 \times 10^{-7} M$$
 $pOH = 6.26$
 $pH = 7.74$

Zinc Hydroxide begins to precipitate at pH = 7.74

$$Zn(OH)_{2(s)} \rightleftharpoons Zn^{2+} + 2OH^{-}$$
 $K_{sp1} = 3 \times 10^{-16}$
 $Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+} + 2OH^{-}$ $K_{sp2} = 7.1 \times 10^{-12}$

Initial Solution has 1.00 mM Zn²⁺ and 1.00 mM Mg²⁺.

II) At what pH is 99.9% of the Zn^{2+} removed from solution?

$$Zn(OH)_{2(s)} \rightleftharpoons Zn^{2+} + 2OH^{-}$$
 $K_{sp1} = 3 \times 10^{-16}$
 $Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+} + 2OH^{-}$ $K_{sp2} = 7.1 \times 10^{-12}$

Initial Solution has 1.00 mM Zn²⁺ and 1.00 mM Mg²⁺.

II) At what pH is 99.9% of the Zn^{2+} removed from solution?

$$[Zn^{2+}] = 1.00 \times 10^{-6} M$$
 $K_{sp1} = [Zn^{2+}][OH^{-}]^{2}$

$$Zn(OH)_{2(s)} \rightleftharpoons Zn^{2+} + 2OH^{-}$$
 $K_{sp1} = 3 \times 10^{-16}$
 $Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+} + 2OH^{-}$ $K_{sp2} = 7.1 \times 10^{-12}$

Initial Solution has 1.00 mM Zn²⁺ and 1.00 mM Mg²⁺.

II) At what pH is 99.9% of the Zn^{2+} removed from solution?

$$[Zn^{2+}] = 1.00 \times 10^{-6}M$$
 $K_{sp1} = [Zn^{2+}][OH^{-}]^{2}$

$$[OH^{-}] = \sqrt{\frac{K_{sp1}}{[Zn^{2+}]}} = \sqrt{\frac{3 \times 10^{-16}}{10^{-6}}} = 1.73 \times 10^{-5}M$$
 $pOH = 4.76$
 $pH = 9.24$

At pH 9.24 we can remove 99.9% of the Zn^{2+}

$$Zn(OH)_{2(s)} \rightleftharpoons Zn^{2+} + 2OH^{-}$$
 $K_{sp1} = 3 \times 10^{-16}$
 $Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+} + 2OH^{-}$ $K_{sp2} = 7.1 \times 10^{-12}$

Initial Solution has 1.00 mM Zn²⁺ and 1.00 mM Mg²⁺.

III) At what pH does Magnesium Hydroxide begin to precipitate?

$$Zn(OH)_{2(s)} \rightleftharpoons Zn^{2+} + 2OH^{-}$$
 $K_{sp1} = 3 \times 10^{-16}$
 $Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+} + 2OH^{-}$ $K_{sp2} = 7.1 \times 10^{-12}$

Initial Solution has 1.00 mM Zn²⁺ and 1.00 mM Mg²⁺.

III) At what pH does Magnesium Hydroxide begin to precipitate?

$$[Mg^{2+}] = 1.00 \times 10^{-3}M$$
 $K_{sp2} = [Mg^{2+}][OH^{-}]^{2}$

$$Zn(OH)_{2(s)} \rightleftharpoons Zn^{2+} + 2OH^{-}$$
 $K_{sp1} = 3 \times 10^{-16}$
 $Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+} + 2OH^{-}$ $K_{sp2} = 7.1 \times 10^{-12}$

Initial Solution has 1.00 mM Zn²⁺ and 1.00 mM Mg²⁺.

III) At what pH does Magnesium Hydroxide begin to precipitate?

$$[Mg^{2+}] = 1.00 \times 10^{-3}M$$
 $K_{sp2} = [Mg^{2+}][OH^{-}]^{2}$

$$[OH^{-}] = \sqrt{\frac{K_{sp2}}{[Mg^{2+}]}} = \sqrt{\frac{7.1 \times 10^{-12}}{10^{-3}}} = 8.43 \times 10^{-5}M$$
 $pOH = 4.07$
 $pH = 9.93$

Magnesium Hydroxide begin to precipitate at pH = 9.93

We can separate Zinc and Magnesium!

Chem M3LC

Diprotic Weak Acids: Sulfuric Acid and Hydrogen Sulfide

$$H_2SO_4 \rightleftharpoons H^+ + HSO_4^- \qquad K_1 = \infty$$

$$HSO_4^- \rightleftharpoons H^+ + SO_4^{2-}$$
 $pK_2 = 1.99$

$$BaSO_4(s)$$
 $K_{sp} = 1.1 \times 10^{-10}$

$$H_2S \rightleftharpoons H^+ + HS^- \qquad pK_1 = 7.02$$

$$HS^- \rightleftharpoons H^+ + S^{2-}$$
 $pK_2 = 13.89$

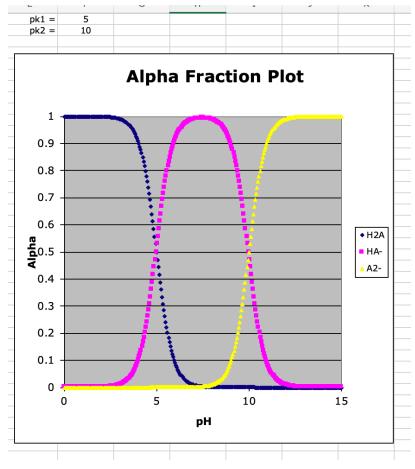
$$CdS(s)$$
 $K_{sp} = 1.0 \times 10^{-27}$

Diprotic Weak Acids: Alpha Fractions

$$H_2A \rightleftharpoons H^+ + HA^- \qquad K_1$$

$$HA^- \rightleftharpoons H^+ + A^{2-} \qquad K_2$$

$$K_1 \gg K_2$$



Diprotic Weak Acid

Constants: K1, K2, Kw, Ctot

Five species: [H2A], [HA-], [A2-], [H+], [OH-]

K1 = [H+][HA-]/[H2A] acid dissociation 1

K2 = [H+][A2-]/[HA-] acid dissociation 2

Kw = [H+][OH-] water dissociation

[H+] = [HA-]+ 2[A2-] + [OH-] charge balance

Ctot = [H2A] + [HA-] + [A2-] mass balance

Alpha Fractions

$$\alpha_{H_2A} = \frac{1}{1 + \frac{K_1}{[H+]} + \frac{K_1K_2}{[H+]^2}}$$

$$\alpha_{HA^-} = \frac{1}{\frac{[H+]}{K_1} + 1 + \frac{K_2}{[H+]}}$$

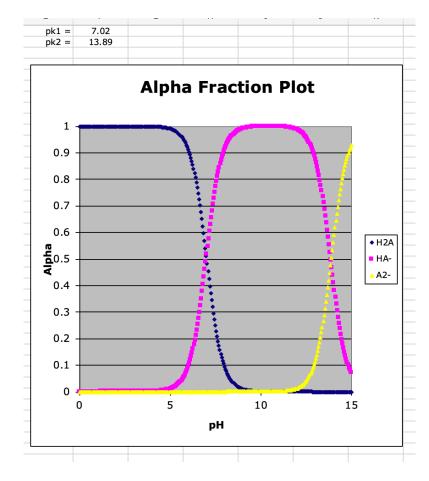
$$\alpha_{A^{2-}} = \frac{1}{1 + \frac{[H+]}{K_2} + \frac{[H+]^2}{K_1K_2}}$$

Diprotic Weak Acids: Alpha Fractions and Exact Solutions

$$H_2S \rightleftharpoons H^+ + HS^- \qquad K_1$$

$$HS^- \rightleftharpoons H^+ + S^{2-}$$
 K_2

$$pK_1 = 7.02$$
 $pK_2 = 13.89$



Alpha Fractions

$$\alpha_{H_2S} = \frac{1}{1 + \frac{K_1}{[H+]} + \frac{K_1K_2}{[H+]^2}}$$

$$\alpha_{SH^{-}} = \frac{1}{\frac{[H+]}{K_1} + 1 + \frac{K_2}{[H+]}}$$

$$\alpha_{S^{2-}} = \frac{1}{1 + \frac{[H+]}{K_2} + \frac{[H+]^2}{K_1 K_2}}$$

$$pH = 13.89$$
 $\alpha_{S^{2-}} = 0.5$

$$pH = 7.02$$
 $\alpha_{S^{2-}} = 1.28 \times 10^{-4}$

Diprotic Weak Acid: Sulfuric Acid

$$H_2SO_4 \rightleftharpoons H^+ + HSO_4^- \qquad K_1 = \infty$$

 $HSO_4^- \rightleftharpoons H^+ + SO_4^{2-} \qquad pK_2 = 1.99$

Can be considered a monoprotic acid

What is the equilibrium concentration of sulfate in a solution with a total sulfuric acid concentration of 0.200 M and a pH of I?

$$\alpha_{SO_4^{2-}} = \frac{1}{1 + \frac{[H+]}{K_2}} = \frac{1}{1 + \frac{10^{-1}}{10^{-1.99}}} = 9.28 \times 10^{-2}$$

$$[SO_4^{2-}] = C_{sulfate}^{tot} \alpha_{SO_4^{2-}} = (0.1)(9.28 \times 10^{-2}) = 9.28 \times 10^{-3} M$$

Diprotic Weak Acids: Sulfuric Acid and Hydrogen Sulfide

$$H_2SO_4 \rightleftharpoons H^+ + HSO_4^- \qquad K_1 = \infty$$

$$HSO_4^- \rightleftharpoons H^+ + SO_4^{2-}$$
 $pK_2 = 1.99$

$$BaSO_4(s)$$
 $K_{sp} = 1.1 \times 10^{-10}$

$$H_2S \rightleftharpoons H^+ + HS^- \qquad pK_1 = 7.02$$

$$HS^- \rightleftharpoons H^+ + S^{2-}$$
 $pK_2 = 13.89$

$$CdS(s)$$
 $K_{sp} = 1.0 \times 10^{-27}$

Cadmium Sulfide Precipitation Reaction - pH Dependence

$$CdS(s) \rightarrow Cd^{2+} + S^{2-}$$

$$K_{sp} = 1.0 \times 10^{-27}$$

$$[Cd^{2+}] = C_{sulfide}^{tot} = \frac{[S^{2-}]}{\alpha_{S^{2-}}}$$

$$total Cd = total S$$

$$[S^{2-}] = \alpha_{S^{2-}}[Cd^{2+}]$$

$$K_{sp} = [Cd^{2+}][S^{2-}]$$

$$[Cd^{2+}] = \sqrt{\frac{K_{sp}}{\alpha_{S^{2-}}}}$$

$$\alpha_{S^{2-}} = \frac{1}{1 + \frac{[H+]}{K_2} + \frac{[H+]^2}{K_1 K_2}}$$

$$pK_1 = 7.02$$

 $pK_2 = 13.89$

Cadmium Sulfide Precipitation Reaction - pH Dependence

$$CdS(s) \rightarrow Cd^{2+} + S^{2-}$$

$$K_{sp} = 1.0 \times 10^{-27}$$

$$[Cd^{2+}] = \sqrt{\frac{K_{sp}}{\alpha_{S^{2-}}}} \qquad \alpha_{S^{2-}} = \frac{1}{1 + \frac{[H+]}{K_2} + \frac{[H+]^2}{K_1 K_2}} \qquad pK_1 = 7.02$$

$$pK_2 = 13.89$$

$$pH = 3$$
 $\alpha_{S^{2-}} = 1.42 \times 10^{-15}$ $[Cd^{2+}] = 8.39 \times 10^{-7} M$

$$pH = 7.0$$
 $\alpha_{S^{2-}} = 1.28 \times 10^{-4}$ $[Cd^{2+}] = 1.26 \times 10^{-10} M$

$$pH = 10.0$$
 $\alpha_{S^{2-}} = 6.30 \times 10^{-8}$ $[Cd^{2+}] = 2.80 \times 10^{-12} M$

Barium Sulfate Precipitation Reaction - pH Dependence

$$BaSO_4(s) \to Ba^{2+} + SO_4^{2-}$$
 $K_{sp} = 1.1 \times 10^{-10}$

$$[Ba^{2+}] = C_{sulfate}^{tot} = \frac{[SO_4^{2-}]}{\alpha_{SO_4^{2-}}}$$
 total Ba²⁺ = total sulfate

$$[SO_4^{2-}] = \alpha_{SO_4^{2-}}[Ba^{2+}]$$

$$K_{sp} = [Ba^{2+}][SO_4^{2-}]$$

$$K_{sp} = [Ba^{2+}][SO_4^{2-}]$$

$$[Ba^{2+}] = \sqrt{\frac{K_{sp}}{\alpha_{SO_4^{2-}}}}$$

$$\alpha_{SO_4^{2-}} = \frac{1}{1 + \frac{[H+]}{K_2} + \frac{[H+]^2}{K_1 K_2}} \approx \frac{1}{1 + \frac{[H+]}{K_2}} \qquad K_1 = \infty$$

$$pK_2 = 1.99$$

Barium Sulfate Precipitation Reaction - pH Dependence

$$BaSO_4(s) \to Ba^{2+} + SO_4^{2-}$$
 $K_{sp} = 1.1 \times 10^{-10}$

$$[Ba^{2+}] = \sqrt{\frac{K_{sp}}{\alpha_{SO_4^{2-}}}} \qquad \alpha_{SO_4^{2-}} \approx \frac{1}{1 + \frac{[H+]}{K_2}} \qquad pK_2 = 1.99$$

$$@pH = 1 \qquad \alpha_{SO_4^{2-}} = 9.28 \times 10^{-2}$$

$$[Ba^{2+}] = 3.44 \times 10^{-5} M$$

Diprotic Weak Acids: Alpha Fractions and Exact Solutions

Exact Solution:

Iterative eqns for [H+]

$$[H+][HA-] = K1[H2A]$$

$$[H+]([H+] - [OH-] - 2[A2-]) = K1[H2A]$$

$$[H+]^2 -2[H+][A2-] - Kw = K1[H2A]$$

$$[H+]^2 = K1[H2A] + 2K2[HA-] + Kw$$

Initial Guess: [H+] = sqrt (K1*Ctot + Kw)

Calculate [H2A], [HA-], [A2-]

$$[H+] = sqrt(K1[H2A] + 2K2[HA-] + Kw)$$

Approximate Solutions:

H₂A solution

$$[H^+] = \sqrt{K_1 C^{tot}}$$
(Ignore K₂)

HA- solution

$$pH = \frac{pK_1 + pK_2}{2}$$
(Ampholyte)

A²- solution

$$[OH^{-}] = \sqrt{K_{b2}C^{tot}}$$
(Ignore K_I)